Do Bond Covenants Prevent Asset Substitution?

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DO BOND COVENANTS PREVENT ASSET SUBSTITUTION?

The Asset Substitution Problem

- ► Levered equity is a *call option* on a firm's underlying assets.
- \Rightarrow Equityholders gain from increasing the riskiness of the firm at the expense of debtholders as first noted by Jensen and Meckling (1976).
- Underlying reason: Limited liability makes equity a *convex function* of the unlevered firm value.

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Potential Solutions:

- Special financial structure: Hybrid debt (convertibles), short-term debt,...
- Bond covenants prohibiting certain actions

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Potential Solutions:

- Special financial structure: Hybrid debt (convertibles), short-term debt,...
- Bond covenants prohibiting certain actions
- New Mechanism: Bond covenants changing the curvature of equity

HOW CAN WE MEASURE ASSET SUBSTITUTION?

Where to look?

- Asset substitution is most likely to have happened with firms that went bankrupt.
- We track firms that have defaulted for the last 84 months before their default.

Empirical Difficulties

- **Endogeneity** of covenant and risk-shifting decision:
 - 1. The riskiness we observe depends on whether covenants are in place or not.
 - 2. The decision to include covenants in bond contracts depends on the expected gains from risk-shifting.
- Identification problem because the standard *leverage effect* leads to an automatic increase in a firm's volatility as it approaches default.
- Standard econometric techniques do not work because of the conditional sample.

HOW CAN WE MEASURE ASSET SUBSTITUTION?

Our Approach

- Structural corporate finance model that links the leverage and the characteristics of the firm to observable equity prices (identification problem).
- Defaulted firms are grouped into two sub-samples
 - 1. firms having issued bonds with covenants attached
 - 2. firms having issued bonds without covenants attached.

and the structural model is estimated separately for each group (endogeneity problem).

 New estimation approach: conditional simulated methods of moments that is able to deal with our sample of defaulted firms (selection bias).

RESULTS: DO COVENANTS PREVENT ASSET SUBSTITUTION?

Firms with bond covenants...

- … have strong risk-shifting incentives (risk-shifting is not costly for equityholders),
- ... and seem to use bond covenants to commit to a more prudent conduct of business. The equity value function is less convex because of the covenant,
- ... engage in risk-shifting very early but not any further in periods of financial distress.

Firms without bond covenants...

- … have low risk-shifting incentives (risk-shifting is very costly),
 ⇒ agency costs imposed on debtholders are relatively small.
- ... exhibit risk-shifting and default strategies that are very close to the optimal behavior as predicted by theory,
- … have optimally chosen to not use covenants because the inefficiencies created through covenants exceed their benefits (agency cost savings).

Results

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Related Literature

Theory on Risk Shifting

- Special financial structure, e.g., hybrid debt in the form of a convertible bond as in Green (1984): The concavity induced by the thread of conversion exactly offsets the convexity induced by limited liability.
 - Problem: works only in a one period model.
- Short-term debt (Djembissi, 2011): Risk-shifting increases the cost of future debt which affects future dividends.
 - Problem: Very costly due to suboptimal leverage and too early default.
 - Empirical evidence: few executives feel that short borrowing reduces risk-shifting incentives, Graham and Harvey (2007).

Empirics on Covenant Use

- Smith and Warner (1979): Costly contracting hypothesis.
- ► Bradley and Roberts (2003), Wei (2005): Covenants reduce the cost the debt.
- Chava et al. (2010), Billett et al (2007): Firms actively use covenants to reduce the agency costs of debt financing (focus on investment).

MODEL - THE FIRM

Capital Structure

- Outstanding debt represented by consol bond with coupon *C*.
- *Bankruptcy costs*: a fraction α of the unlevered firm value.
- Default happens when X_t hits a predetermined threshold X_D. The threshold is either determined optimally by equityholders or through bond covenants.

Earnings and Assets

Operating income under the risk-neutral measure:

$$dX_t = \mu_i X_t dt + \sigma_i X_t dW_t$$

Value of the unlevered assets (if no risk-shifting occurs):

$$A(X_t) = E^{Q} \left[\int_t^\infty (1 - T_C) e^{-r(s-t)} X_s ds \right] = \frac{(1 - T_C) X_t}{r - \mu}$$

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ASSET SUBSTITUTION

- Equityholders have the option to increase the riskiness of the firm's cashflow:
 σ_i ∈ {σ_L, σ_H} where 0 < σ_L < σ_H < ∞
- ► Increasing the risk of the cashflow can be **costly**:

 $\mu_i \in \{\mu_L, \mu_H\}$ where $\mu_H \leq \mu_L < \infty$

- expenses necessary for establishing and upholding the riskier use of the assets and/or
- increase in the discount rate
- ⇒ **Risk-shifting can destroy value**:

$$A_H(X_t) = \frac{(1 - T_C)X_t}{r - \mu_H} \le \frac{(1 - T_C)X_t}{r - \mu_L} = A_L(X_t)$$

► Equityholders choose an optimal **risk-shifting threshold** *X*_{*RS*}.



ASSET SUBSTITUTION: OPTIMAL STRATEGIES EQUITYHOLDERS CHOOSE AN OPTIMAL RISK-SHIFTING (X_{RS}) AND DEFAULT THRESHOLD (X_D) .



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- ► Equityholders choose an optimal **risk-shifting threshold** *X*_{*RS*}.
- ► The **convexity** of equity value function induces the risk-taking behavior.



ASSET SUBSTITUTION: CONVEXITY THE CONVEXITY OF THE EQUITY VALUE FUNCTION INCREASES THE MORE FINANCIALLY DISTRESSED THE FIRM BECOMES (LOW VALUES OF X_t)



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- ► The **convexity** of equity value function induces the risk-taking behavior.
- ► The Dilemma:
 - Risk-shifting transfers value from debtholders to equityholders.

INTRODUCTION	Methodology	Results
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ASSET SUBSTITUTION: VALUE TRANSFER Risk-shifting transfers value from the debtholders to equityholders.



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- ► The Dilemma:
 - Risk-shifting transfers value from debtholders to equityholders.
 - When issuing debt, equityholders would like to commit to not engage in asset substitution but this is not time consistent.

INTRODUCTION	Methodology	Results
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ASSET SUBSTITUTION: LOWER DEBT CAPACITY DEBT CAPACITY IS LOWER DUE TO RISK-SHIFTING.



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CASHFLOW BASED COVENANTS: CONCAVE EQUITY



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CASHFLOW BASED COVENANTS: NO TRANSFER



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 - ... and higher debt capacity, i.e., gains from larger tax shield.

Cashflow Based Covenants: Higher Debt Capacity



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 - There exists a lower technical default threshold just high enough to destroy equityholders risk-shifting incentives but is not contractible upon.
 - Real world solution: Renegotiate cashflow covenants such that default does not happen too early.

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THE OPTIMAL DEBT CONTRACT

- A covenant is not costless (costly contracting hypothesis, Smith and Warner, 1979) but creates inefficiencies through limiting the choice set of management.
- A cashflow covenant creates **inefficiencies through too early default**.
- If the valuation consequences of asset substitution are high, equityholders will engage in risk-shifting only in very bad times which is a low probability event.
- Thus, the expected value of the agency costs that are priced into debt is relatively low.
- In that case, the value loss due to the inefficiencies created by the covenant might outweigh the agency costs induced by asset substitution.

INEXPENSIVE (1st row) AND **EXPENSIVE** RISK-SHIFTING (2nd row)



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OUR ESTIMATION APPROACH

- The structural model links observable equity prices to leverage and unobservable firm characteristics which are estimated.
- No optimizing behavior is imposed:
 - The optimal risk-taking (and default) behavior is not hard-wired in our econometric model.
 - The data determines the risk-shifting threshold X_{RS} and the default threshold X_D .
- Parameters to be estimated: $b = [\sigma_L, \sigma_H, \mu_L, \mu_H, \alpha_L, \alpha_H, \zeta_{RS}, \zeta_D]$
 - cashflow volatilities $[\sigma_L, \sigma_H]$;
 - cashflow growth rate under the Q-measure $[\mu_L, \mu_H]$;
 - cashflow growth rate under the P-measure $[\alpha_L, \alpha_H]$;
 - ► risk-shifting and default threshold ($[X_{RS}, X_D]$), defined as a multiple ($[\zeta_{RS}, \zeta_D]$) of outstanding debt;

Problem: SAMPLING CONDITIONAL ON DEFAULT CREATES DEPENDENCE



INTRODUCTION	Methodology	Results
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INTRODUCTION	Methodology	Results
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Standard Simulated Methods of Moments

1. Simulate a large sample of companies.

Solution: CONDITIONAL SIMULATED METHODS OF MOMENTS

- 1. Simulate a large sample of companies.
- 2. Choose different moments which describe the simulated sample, e.g. mean and variance of the equity and implied cash-flow returns.

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- ► Instead of simulating forward we **simulate back in time**.
- Instead of a starting point to begin with we have an end-point (default threshold, X_D) to end at.

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Modification

- ► Instead of simulating forward we **simulate back in time**.
- Instead of a starting point to begin with we have an end-point (default threshold, X_D) to end at.
- Instead of iid draws we employ the appropriate conditional joint distribution for the observations prior to default.

INTRODUCTION	Methodology	Results

DATA

- Sample of 176 firms that have defaulted between 2000 and 2013 (from Capital IQ).
- Stock price and accounting data from 1993 to 2013 (from Capital IQ).
- Bond covenant information (from Mergent FISD).

We follow Chava et al. (2010) and classify covenants into four groups:

- 1. Investment restrictions (89% of bonds)
- 2. Subsequent financing restrictions (86%)
- 3. Event related restrictions (83%)
- 4. Dividend and other payment restrictions (66% vs 14% in the sample of non-defaulted firms in Chava et al. (2010))

Descriptive statistics for bonds outstanding

COVENANTS REDUCE THE CREDIT SPREAD

	mean	p25	median	p75
Bonds with covenants (59%)				
Offering amount (mil)	256.05	100	175	300
Treasury spread (b.p.)	137.84	0	81	222
Maturity (in months)	128.74	84	117	121
Issuance time before default (in months)	100.64	45	84	147
Security level	3.77	3	4	4
Bonds without covenants (41%)				
Offering amount (mil)	200.63	90	150	275
Treasury spread (b.p.)	345.55	0	388	556
Maturity (in months)	124.40	84	120	121
Issuance time before default (in months)	120.21	52	81	162
Security level	3.88	3	4	4

INTRODUCTION	Methodology	Results
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FINDINGS: FIRMS WITH BOND COVENANTS...

- ... can considerably increase the cashflow risk and risk-shifting is not costly.
- \Rightarrow ... have a high risk-shifting incentive.

parameter		low risk	high risk	
cashflow volatili	ty	$\sigma_L = 0.20$	$\sigma_H = 0.51$	
cashflow growth	under Q	$\mu_L = -0.06$	$\mu_H = -0.0622$	
threshold	estimated	if no coven	ants were in plac	ce
default (X_D)	0.96		0.37	
risk shifting (X_{RS})	23.96		9.19	
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Methodology	Results
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FINDINGS: FIRMS WITH BOND COVENANTS...

- ... can considerably increase the cashflow risk and risk-shifting is not costly.
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 - … have a default threshold that is very close to the cashflow covenant X_D = C = 1, as expected which considerably reduces the convexity of the equity function.

parameter		low risk	high risk
cashflow volatility		$\sigma_L = 0.20$	$\sigma_H = 0.51$
cashflow growth under ${\mathbb Q}$		$\mu_L = -0.06$	$\mu_{H} = -0.0622$
threshold	estimated	if no coven	ants were in place
default (X _D)	0.96		0.37
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INTRODUCTION	Methodology	Results
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FINDINGS: FIRMS WITH BOND COVENANTS...

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- … have a default threshold that is very close to the cashflow covenant X_D = C = 1, as expected which considerably reduces the convexity of the equity function.
- … have a very high risk-shifting threshold. Many firms are already in the high risk-regime at the beginning of our sample period. Our interpretation: They don't increase riskiness of the firm any further in financial distress (close to X_D)

parameter	low risk	high risk
cashflow volatility	$\sigma_L = 0.20$	$\sigma_H = 0.51$
cashflow growth under ${\mathbb Q}$	$\mu_L = -0.06$	$\mu_H = -0.0622$

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INTRODUCTION	Methodology	Results
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FINDINGS: FIRMS WITHOUT BOND COVENANTS...

- ... can considerably increase the cashflow risk but risk-shifting is very costly ($\mu_L \mu_H = 3\%$ vs 0.2% for firms with covenants).
- \Rightarrow ... have low risk-shifting incentives. Risk-shifting takes place just prior to default.

	without	covenants	with covenants	
parameter	low risk	high risk	low risk	high risk
cashflow volatility	$\sigma_L = 0.37$	$\sigma_H = 0.86$	0.20	0.51
cashflow growth under \mathbb{Q}	$\mu_L=0.02$	$\mu_H=-0.01$	-0.06	-0.0622

	without covenants		with cov	enants
threshold	estimated	optimal	estimated	optimal
default (X_D)	0.10	0.196	0.96	0.37
risk shifting (X_{RS})	0.35	0.204	23.96	9.19

FINDINGS: FIRMS WITHOUT BOND COVENANTS...

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- ⇒ … have low risk-shifting incentives. Risk-shifting takes place just prior to default.
- ... shift the risk and declare default very closely to the optimal threshold.

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parameter	low risk	high risk	low risk	high risk
cashflow volatility	$\sigma_L = 0.37$	$\sigma_H = 0.86$	0.20	0.51
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- ⇒ … have low risk-shifting incentives. Risk-shifting takes place just prior to default.
- ... shift the risk and declare default very closely to the optimal threshold.
- … have optimally chosen to not use bond covenants.

	without covenants		with covenants	
parameter	low risk	high risk	low risk	high risk
cashflow volatility	$\sigma_L = 0.37$	$\sigma_H = 0.86$	0.20	0.51
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FIRMS WITHOUT BOND COVENANTS HAVE ISSUED THE OPTIMAL CONTRACT



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CONCLUSION

We use a structural corporate finance model and a new estimation technique to answer whether bond covenants prevent asset substitution.

We find that

- Firms with strong risk-shifting incentives employ covenants to reduce risk-shifting incentives.
- Covenants prevent that these firms engage in risk-shifting during periods of financial distress.
- The mechanism at work is that covenants decrease the convexity of the equity value function.
- Firms without covenants have low risk-shifting incentives
- and optimally chosen not to use covenants.